Notes: 1. Solve all the questions.
2. Each question carry equal marks.

UNIT - I

1. a) Show that any covariant tensor of the second order may be expressed as the sum of symmetric \& skew symmetric tensor.
b) Show that if $A^{m}$, Bnrs are tensors then $A^{m} B m r s$ is also a tensor.

## OR

c) Show that $\frac{\mathrm{dg}}{\mathrm{g}}=\mathrm{g}^{\mathrm{mn}} \mathrm{dg}_{\mathrm{mn}}=-\mathrm{g}_{\mathrm{mn}} \mathrm{dg}^{\mathrm{mn}}$
d) Show that an element of volume $g^{\frac{1}{2}} \mathrm{dx}^{1} \mathrm{dx}^{2}----\mathrm{dx}^{\mathrm{N}}$ is invariant.

## UNIT - II

2. a) Show that $g_{r}^{m n}=-g^{m s} \nabla_{\mathrm{sr}}{ }^{n}-g^{\mathrm{sn}} \widetilde{\mathrm{sr}}^{\mathrm{m}}$.

6
b) Compute the nonvanishing Christoffel symbols of second kind for

$$
\mathrm{ds}^{2}=\mathrm{dr}^{2}+\mathrm{r}^{2} \mathrm{~d} \theta^{2}+\mathrm{r}^{2} \sin ^{2} \theta \mathrm{~d} \phi^{2}
$$

## OR

c) Prove that $\frac{\delta \mathrm{A}}{\delta \mathrm{u}}=\frac{\mathrm{dA}}{\mathrm{du}}$ for a scalar A.
d) Show that under a linear transformation of a coordinate system
$x^{m}=a_{n}^{m} x^{\prime n}+b^{m}, a_{n}^{m}, b^{m}$ are constants, the Christoffel symbols are tensors.
UNIT - III
3. a) Obtain the transformation equations for mass.
b) Obtain the transverse \& longitudinal mass.
c) A particle is given a kinetic energy equal to $n$ times its rest energy $\mathrm{m}_{\mathrm{o}} \mathrm{C}^{2}$ what are its speed \& momentum?
d) Find the expression for four velocity in component form.

## UNIT - IV

4. a) Obtain wave equation for propagation of magnetic field strength.
b) Obtain expression for transformation of charge density.

## OR

c) Show that the energy momentum tensor of electromagnetic field is trace free.
d) Prove that: $\overline{\mathrm{E}}^{\prime} \cdot \overline{\mathrm{H}}^{\prime}=\overline{\mathrm{E}} \cdot \overline{\mathrm{H}} \& \mathrm{E}^{\prime 2}-\mathrm{H}^{\prime 2}=\mathrm{E}^{2}-\mathrm{H}^{2}$.
5. Solve any six:
a) Define the inner product of tensors. 2
b) Define the contraction of tensor.
c) define Christoffel symbols.
d) Show that $\delta_{\mathrm{n} ; \mathrm{r}}^{\mathrm{m}}=0$
e) Show that $P^{2}-E^{2} / C^{2}=-m_{0}^{2} C^{2}$
f) Define the four force. 2
g) State the Lorentz gauge condition. 2
h) Define the electromagnetic field tensor Fij. 2

